

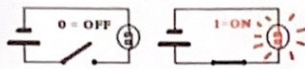
Bobitskaya M. 254



Massachusetts Institute of Technology (MIT)



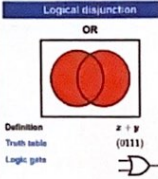
Lecture by Pr. Bob Gallagher  
Boole (1815-1864) & Shannon (1916-2001)



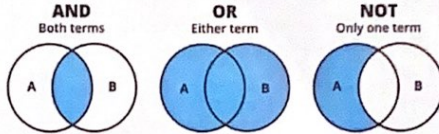
Logical addition  
(disjunction)

A	B	F=A∨B
0	0	0
0	1	1
1	0	1
1	1	1

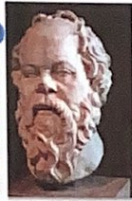
A	B	A ∨ B
True	True	True
True	False	True
False	True	True
False	False	False



BOOLEAN LOGIC

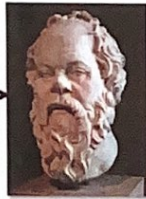


Good logic



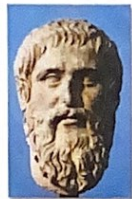
Socrates

Socrates was a philosopher



Socrates

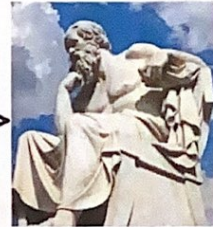
philosophers are men



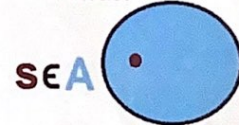
Plato



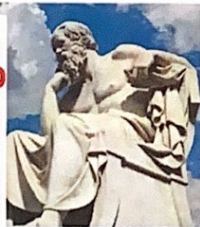
Aristotle



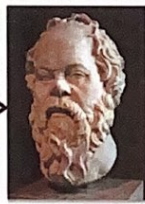
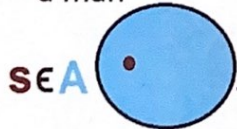
Socrates was a man



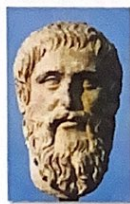
Bad logic



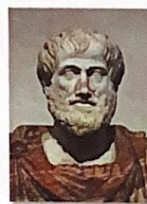
Socrates was a man



Socrates

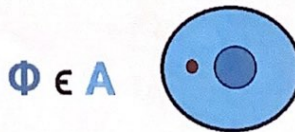


Plato



Aristotle

philosophers are men



Socrates

Socrates was a philosopher



буду.

10 (десять)

*Handwritten signature*

*Handwritten signature*

20

Resume of Lecture by Pr. Bob Gallager from MIT  Massachusetts Institute of Technology (MIT)

George Boole (1815-1864) developed Boolean logic

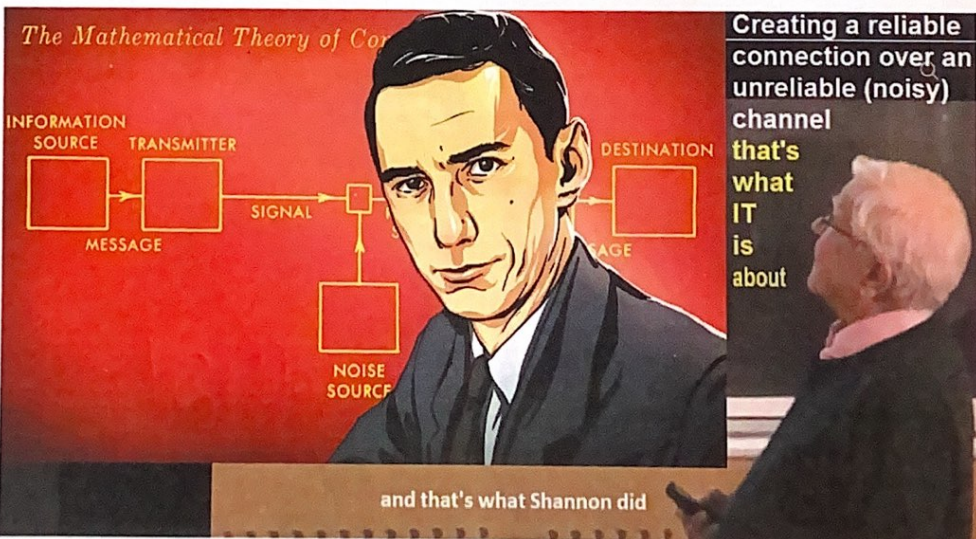
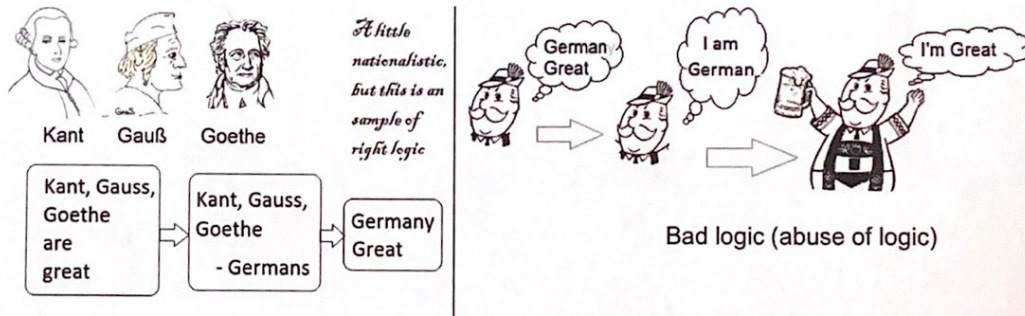
The principles of logical thinking have been understood (and occasionally used) since the Hellenic era.

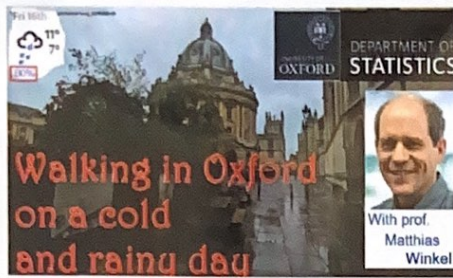
Boole's contribution was to show how to systemize these principles and express them in equations (called Boolean logic or Boolean algebra).

Claude Shannon (1916-2001) showed how to use Boolean algebra as the basis for switching technology. This contribution systemized logical thinking for computer and communication systems, both for the design and programming of the systems and their applications.

Logic continues to be abused in politics, religion and most non-scientific areas

Logic continues to be abused in politics, religion, and most non-scientific areas.





**80% chance of rain**  
says the Met Office in its weather forecast for Oxford.

### CHALK + TALK

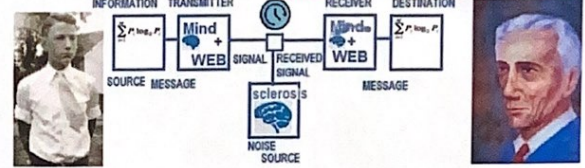


### ink + think



**Good way** ① listening  
② first way of processing

③ Writing, incl. sth. you're not quite sure about

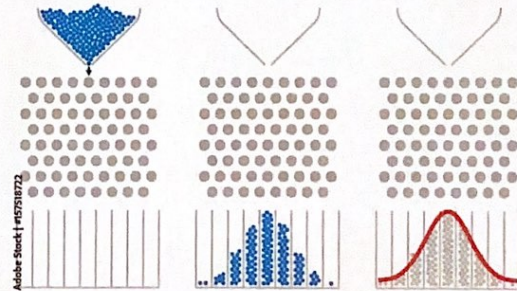
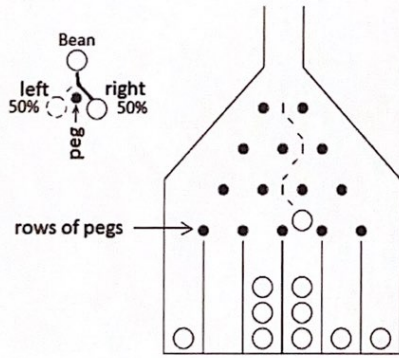


### Markoff Chain Probability Model

for Oxford Weather



If it is Rainy today => there is an 80% chance that it will be rainy tomorrow.



School  $\downarrow$  gravity  $\downarrow$  **MOTION** == formalism ==> University  $E = MC^2$   $\Phi = \int \vec{v} \cdot d\vec{r}$   $w = 2uf$   $\int \int \int d\vec{r}$

Motivation: 80% chance of rain  
Let  $A_j$  be the event of rain at Jam on day  $j$  of this term,  $1 \leq j \leq n$   
Suppose the events  $A_j$  each have probability  $p$ , independently

Oxford				
Tue 13th	Wed 14th	Thu 15th	Fri 16th	
10° 9°	13° 10°	13° 8°	11° 7°	
70%	70%	70%	00%	

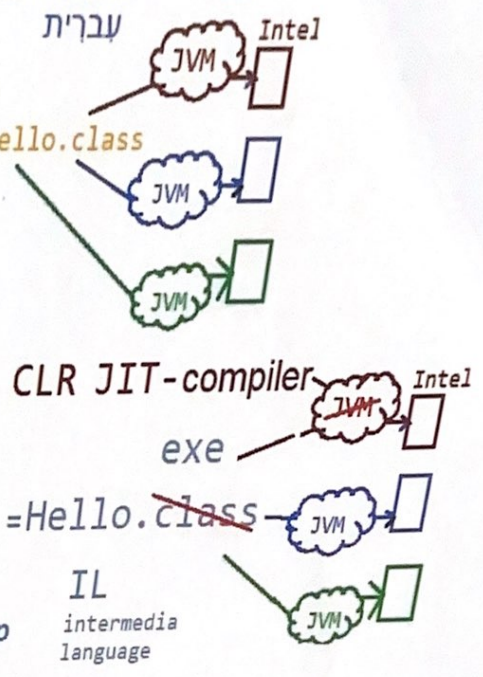
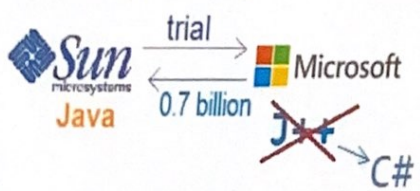


then take notes on the lecture yourself



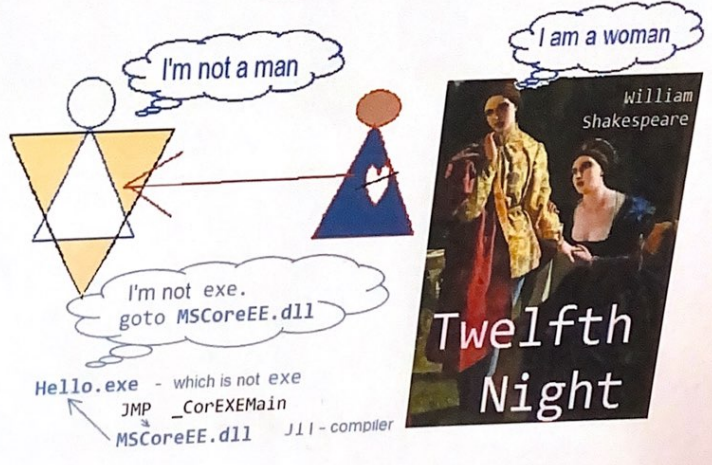
**Cross-platform Java**

Hello.java => javac.exe = Hello.class



Hello.vb => **vbc.exe** = ~~Hello.class~~.exe  
 VB компилятор

Hello.pl => **plc.exe** = ~~Hello.class~~.exe



Jarvishevich. Oxford Lecture  
50% chance of rain at 9 am  
on the day  $j$ :

+1.1 to exam +0.2 +0.5

Suppose the event  $A$  have probabilities independently  $(P) \rightarrow 0, 1, \dots, 0, 9$   
 $0 \leq j \leq n \rightarrow 30, 40$  days

1. Event and probabilities:

Consider an "experiment" which has a set of  $\Omega$  of outcomes  
in  $\Omega$  - sample space

a) tossing a coin  $\Omega = \{H|T\}$

b) throw a dice:  $\square \square$   
max tail

$\Omega = \{(i, j), i, j \in [1, 2, 3, 4, 5, 6]\}$

A subset of  $\Omega$  is called an event

For example

a) a coin comes up tail  $A = \{T\}$

b) We observe of total 9

$A = \{(3, 6), (4, 5), (5, 4), (6, 3)\} \square \square$

If we  $\omega$  is the outcome, we say that event  $A$  occur if  $\omega \in A$

Compliment of  $A$ :

$A^c$  occurs if  $A$  doesn't occur

Union  $A \cup B$  occur if  $A$  or  $B$  occurs (or both)

Intersection:  $A \cap B$

occurs if both  $A$  and  $B$  occurs

Set difference:  $A \setminus B = A \cap B^c$  occur if  $A$  occurs and  $B$  doesn't occurs

$A$  and  $B$

disjoint  $A \cap B = \emptyset$  i.e.  $A$  and  $B$  cannot occur together

We assign a probability  $P(A)$  of each  $A$

Simplest case:

$\Omega$  is finite and all outcomes are equally likely, then  $P(A) = \frac{|A|}{|\Omega|}$

a)  $\left\{ \begin{array}{l} |\Omega| = 2 \\ |A| = 1 \end{array} \right\} \Rightarrow P(A) = \frac{1}{2}$

b)  $\left\{ \begin{array}{l} |\Omega| = 36 \\ |A| = 4 \end{array} \right\} \Rightarrow P(A) = \frac{4}{36} = \frac{1}{9} \square \square \leftarrow \text{queen}$

Elementary Combinatorics:

Arrangement of distinguishable object. Suppose we have a distinguishable objects  
 $n=3$   $(\uparrow \uparrow \uparrow)$ . How many ways are there to order them?

$\Omega = 3! = 3 \cdot 2 \cdot 1 = 6$

Example: There are  $6!$  ways to order the letters of GALOIS. If we randomly reorder the letters what is the probability that vowels are all before consonants?

$$\frac{3!3!}{6!}$$

2) Arrangements when not all objects are indistinguishable.

How many different arrangements of AAA B C D

A is repeated      3 are distinguishable

$$\frac{6!}{3!} = \frac{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6}{3 \cdot 2 \cdot 1} = 120$$

хор мурорак  
не мей мие ефор

РѢТА

Бабушка Маргарита Станиславовна

от Юли  
♡

$$+ 0,1 + 0,1 + 0,1$$

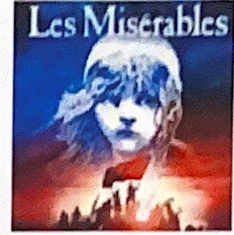
É. Galois (1811-1832) Les Misérables | Do You Hear the People Sing?



Example

There are  $6!$  ways to order the letters of GALOIS

If randomly reorder the letters what is probability that the vowels (A, O, I) are all before consonants (G, L, S)?



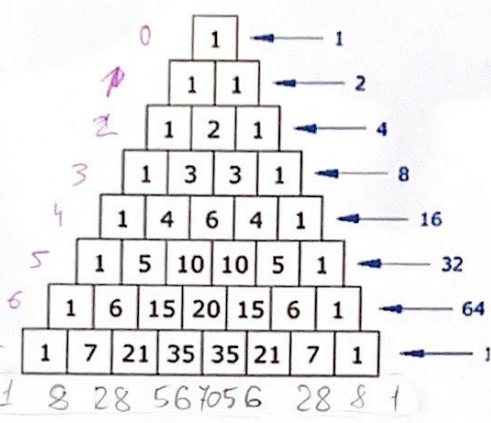
$$3! 3!$$

~~PE~~

$$P = \frac{3! 3!}{6!}$$

puta  
♡

4



### Shannon Hartley Theorem

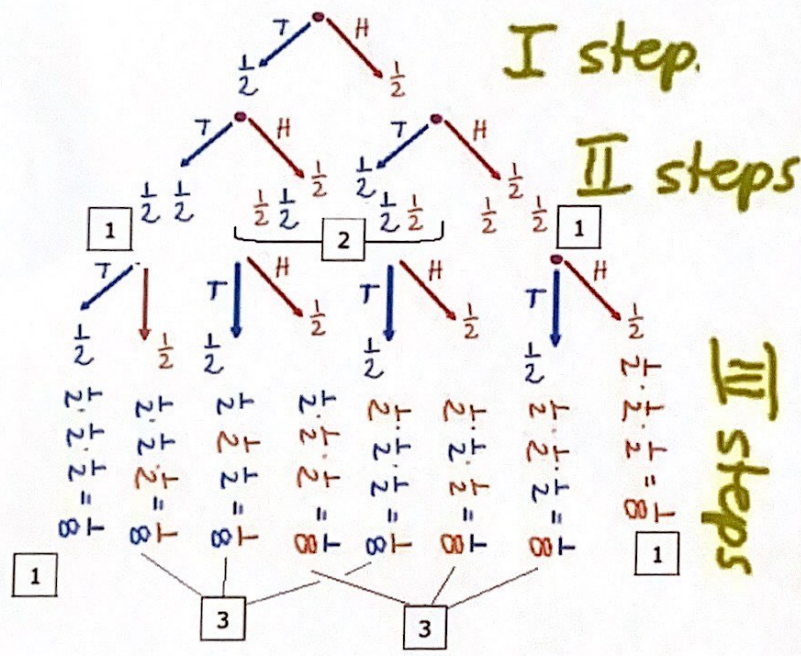
This is a measure of the *capacity* on a channel; it is impossible to transmit information at a faster rate without error.

$$C = B \log_2(1 + S/N)$$

- C = capacity (in bit/s)
- B = bandwidth of channel
- S = signal power (in W)
- N = noise power (in W)

It is more usual to use SNR (in dB) instead of power ratio (as with terrestrial and commercial communications systems)  $S/N \gg 1$ , then rewriting in terms of  $\log_{10}$ .

$$C = B \frac{\log_{10}(S/N)}{\log_{10} 2} = B \frac{10 \log_{10}(S/N)}{10 \cdot \log_{10} 2} = B \frac{SNR}{3.01}$$



$$\begin{aligned} (a + b)^0 &= 1 \\ (a + b)^1 &= a + b \\ (a + b)^2 &= a^2 + 2ab + b^2 \\ (a + b)^3 &= a^3 + 3a^2b + 3ab^2 + b^3 \\ (a + b)^4 &= a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4 \\ (a + b)^5 &= a^5 + 5a^4b + 10a^3b^2 + 10a^2b^3 + 5ab^4 + b^5 \end{aligned}$$

$$(1 + x)^7 = 1 + 7x + 21x^2 + 35x^3 + 35x^4 + 21x^5 + 7x^6 + x^7$$

$\binom{7}{0} \binom{7}{1} \binom{7}{2} \binom{7}{3} \binom{7}{4} \binom{7}{5} \binom{7}{6} \binom{7}{7}$

$$(y + x)^7 = y^7 + 7y^6x + 21y^5x^2 + 35y^4x^3 + 35y^3x^4 + 21y^2x^5 + 7yx^6 + x^7$$

+0.2 Exam



$ABBA = \frac{4!}{2!2!} = \frac{24}{4} = 6$ . The number of arrangements of the  $N$  obj

♡  $\underbrace{x_1 \dots x_1}_{m_1}, \underbrace{x_2 \dots x_2}_{m_2}, \dots, \underbrace{x_k \dots x_k}_{m_k}$

where  $n = m_1 + m_2 + \dots + m_k$

**What should you do in class:**

0. Come up with a good name for your site.

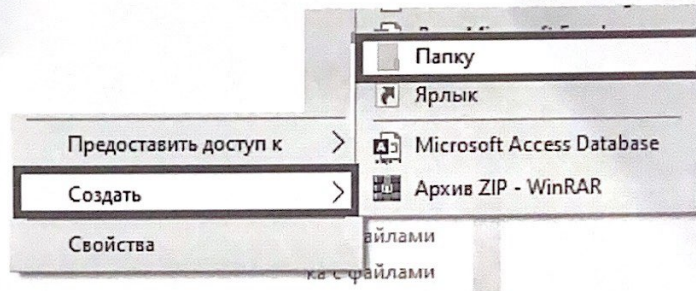
I came up with a name for my site - Confucius (in my opinion, this is a good name)

[www.confucius.bsite.net](http://www.confucius.bsite.net)

1. On a disk or on a flash drive, make a folder that matches the name of the site

[www.confucius.bsite.net](http://www.confucius.bsite.net)

Новый том (D:) >



2. In a folder **D:\www.confucius.bsite.net\** create a folder for Projects

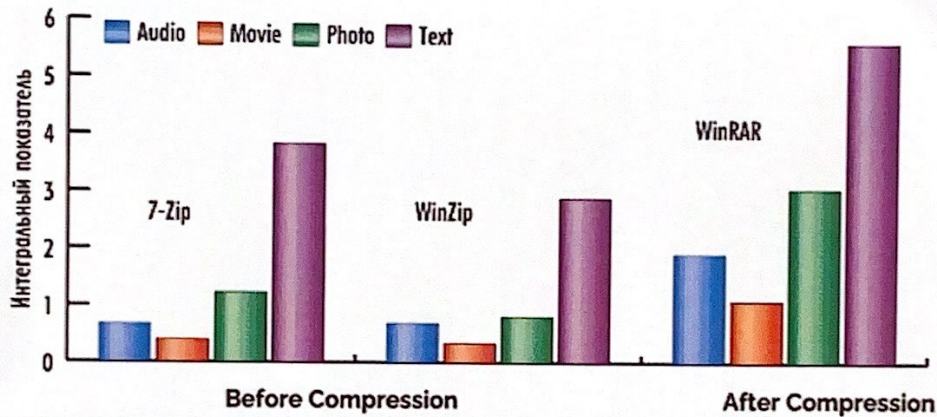
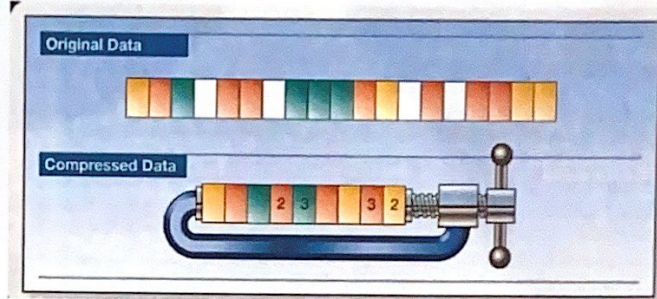
**D:\www.confucius.bsite.net\Projects**

3. In a folder **D:\www.confucius.bsite.net\Projects** create a folder for Projects Number 0

**D:\www.confucius.bsite.net\Projects\0\**

4. In a folder **D:\www.confucius.bsite.net\Projects\0\** create file *index.htm*

# Comparison of the compression ratio of popular archivers



Data	Symbol	Frequency	Symbol	Bit Code
AAAAAAABCCCCCDEEEEE	A	7	A	00
	B	1	B	111
	C	6	C	01
	D	2	D	110
	E	5	E	10

Entropy compression ratio

Before Compression - 21 x 8 bits = 198 bits  
 After Compression - 7 x 2 bits + 1 x 3 bits + 6 x 2 bits + 2 x 3 bits + 5 x 2 bits = 45 bits

$\log_2(64) = 2$  — (+0.3 to Exam) !!!

**What should you do at home:**  
 Register free hosting on **freeasphosting.net**  
 At home because many hosting services do not register from one IP address.

freeasphosting.net

## ASP.NET Hosting .NET 7

**FREE** ASP.NET Hosting  
**FREE** Domain Hosting  
**FREE** MS SQL Database  
**INCLUDES** .NET Core  
**Full Trust Permissions**

**SIGN UP FOR FREE**

**Create Your Free Site**

✉ Confucius@studentweb.cc

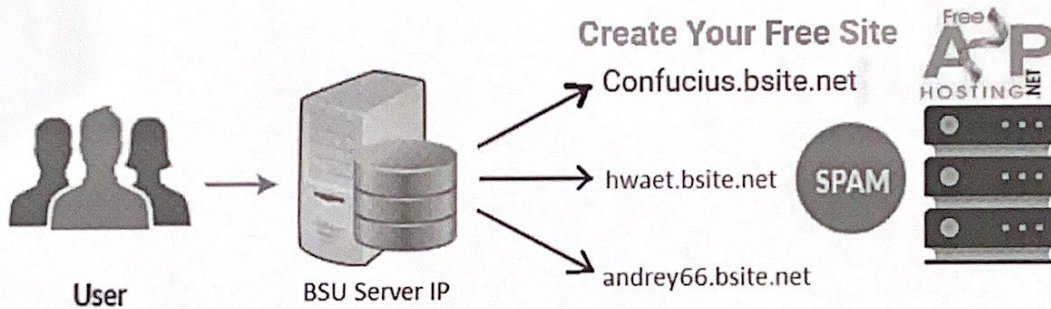
👤 https://Confucius.bsite.net

🔒 .....

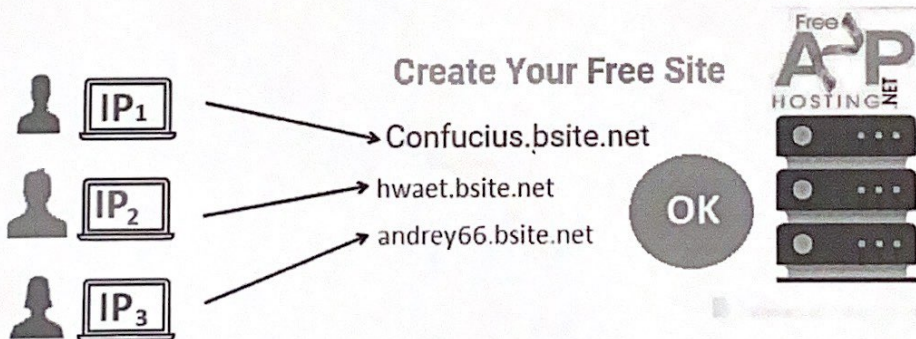
By signing up with our service you agree to our [Terms & Conditions](#).

Create Site

If several dozen hosting attempts to register from one IP address, the **freeasphosting.net** server may decide that this is a SPAMmer and block it.



And if registration is carried out from different computers (with different IP addresses), then the freeasphosting.net server does not raise any suspicions.



After you have registered on the server, send me your address (which you received during registration) by email.

Babitskaya 254



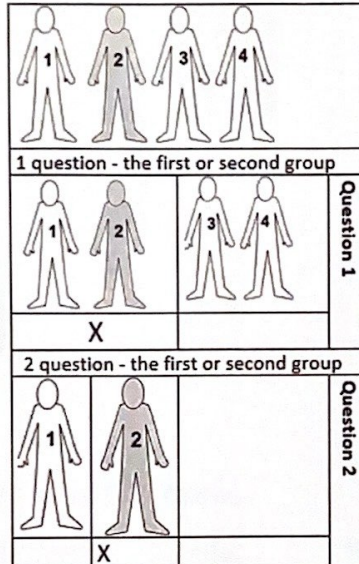
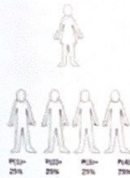
Say **NO** to the first



Say **YES** to the second if it is better than the first



Say **NO** to the third only if it is worse than all the others



Average number of questions =  $2 \cdot 0.25 + 2 \cdot 0.25 + 2 \cdot 0.25 + 2 \cdot 0.25 = 2$

Average number of questions =

$1 \cdot 0.5 +$	$2 \cdot 0.25 +$	$3 \cdot 0.125 +$	$3 \cdot 0.125$

Question 1. Is this Zuckerberg?	50%	$1 \cdot 0.5$
Question 2. Is this Sergey Brin?	25%	$2 \cdot 0.25$
Question 3. Is this Stefan from BMW?	12,5%	$3 \cdot 0.125$
So Prince Saud	12,5%	$3 \cdot 0.125$
Average number of questions =		<b>1,75</b>

Quantifying information

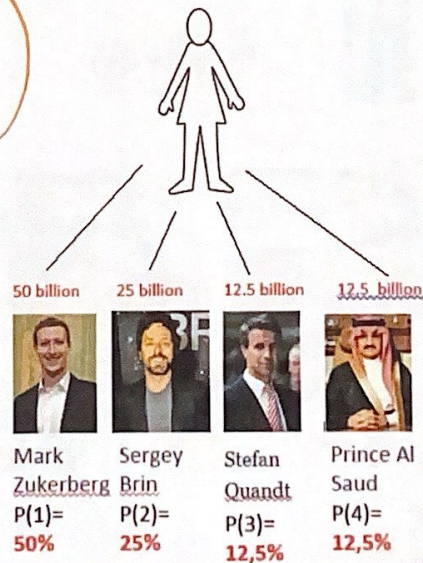
$$S(x) = \sum_{i=1}^n p(i) \log_2 \frac{1}{p(i)}$$

Quantifying information

$$I(x_i) = \log_2 \left( \frac{1}{p_i} \right)$$

number of bits required to encode choice

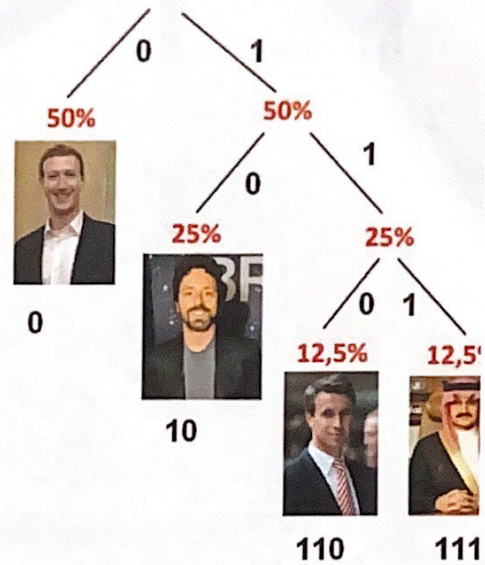
+ 0.5 to Exam



ce

Babitskaya 254

11



First-order approximation  
(symbols independent but with  
frequencies of Belarusian txt).

Мама мыла ра		
М - 3	— 30%	1-3 М
а - 4	— 40%	4-7 а
ы - 1	— 10%	8 -ы
л - 1	— 10%	9 -л
р - 1	— 10%	10 -р
10		
лла <span style="border: 1px solid red; padding: 2px;">мама</span> р		

Мама мыла ра

Ма - 2	22%	1-2	ма
ам - 2	22%	3-4	ам
мы - 1	11%	5	мы
ыл - 1	11%	6	ыл
ла <sub>1</sub> - 1	11%	7	ла
ар - 1	11%	8	ар
ра - 1	11%	9	ра
9			

Second-order approximation (digram (2-symbols) structure as in Belarusian)



0. 4 6 7 3 1 9 1 6 7 3 5  
 ам ыл ла ам ма ра ма ыл ла ам мы  
 мылла рама

